

Evolution of MHD waves in low layers of a Coronal Hole

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Motivation

The formation of small scales in coronal holes has already been studied by several authors: e.g., Matthaeus et al. 1999; Verdini and Velli, 2007; Verdini et al., 2009; Verdini et al. 2010.

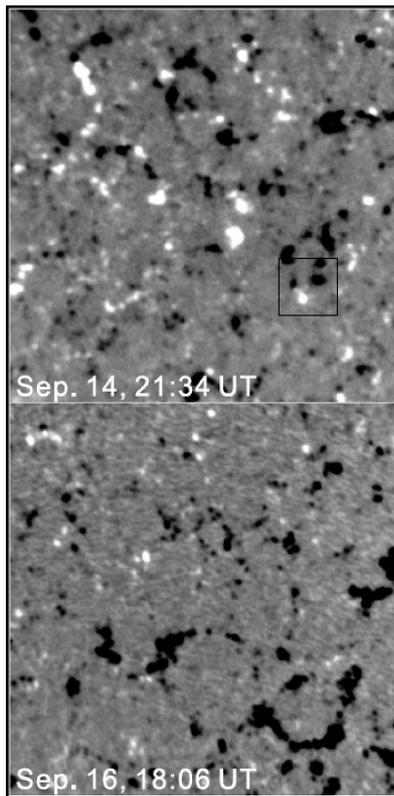
All these studies consider the formation of small scales in a wide region extending beyond the sonic point, considering a unipolar magnetic field.

We would like to investigate if inhomogeneities at the base of the Corona could be responsible for small scale formation at low altitudes.

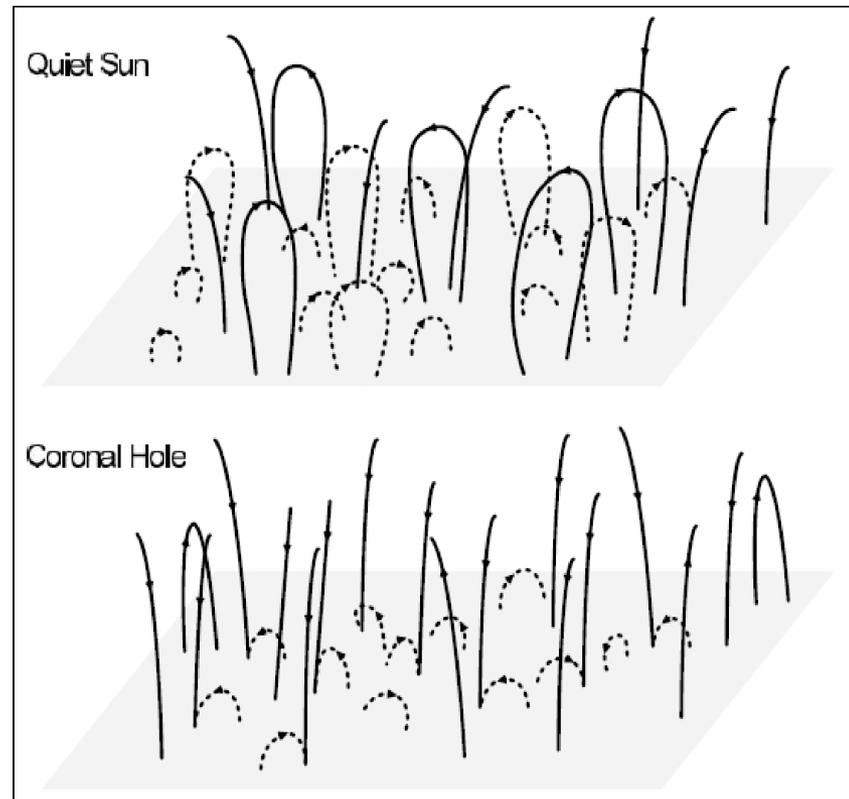
Coronal holes

Coronal holes are low density regions of the solar Corona, mainly situated at poles, where the magnetic field has a dominant polarity but with the presence of regions in the photosphere with inverted polarity.

Quiet Sun



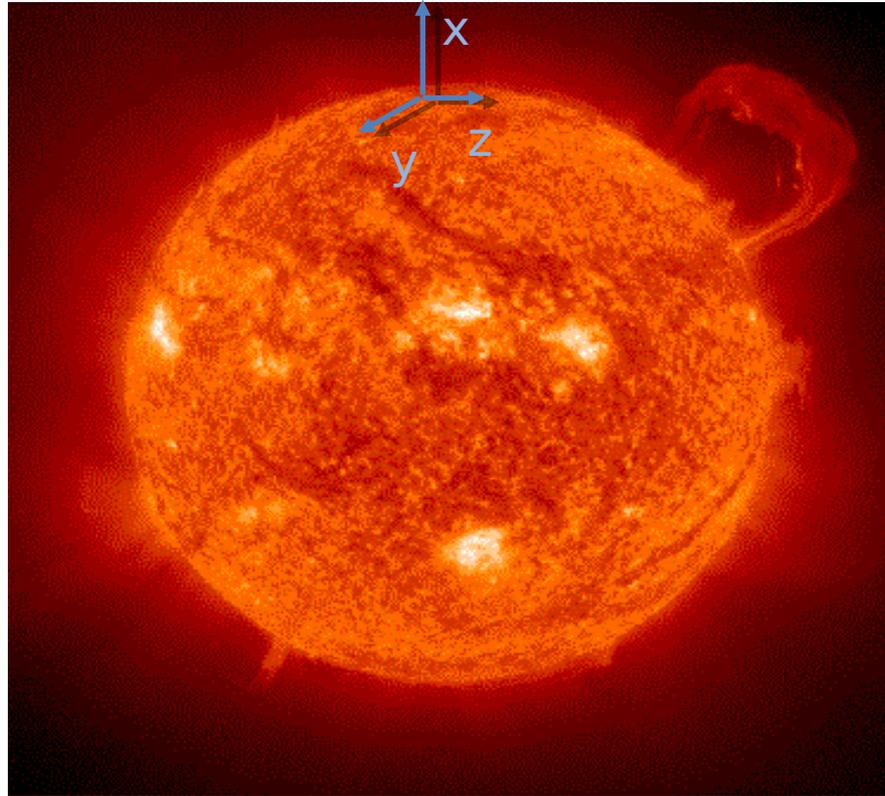
Coronal Hole



A magnetogram (on the left) and a cartoon (on the right) of the magnetic field in a Quiet Sun region and in a Coronal hole. (Zhang, Ma & Wang, ApJ 2006)

A model for the magnetic field in a coronal hole

The reference frame we are considering is situated in this way:



We make two assumption:

- equilibrium potential magnetic field (null current)

$$\vec{B} = -\nabla\phi \quad \longrightarrow \quad \nabla^2\phi = 0$$

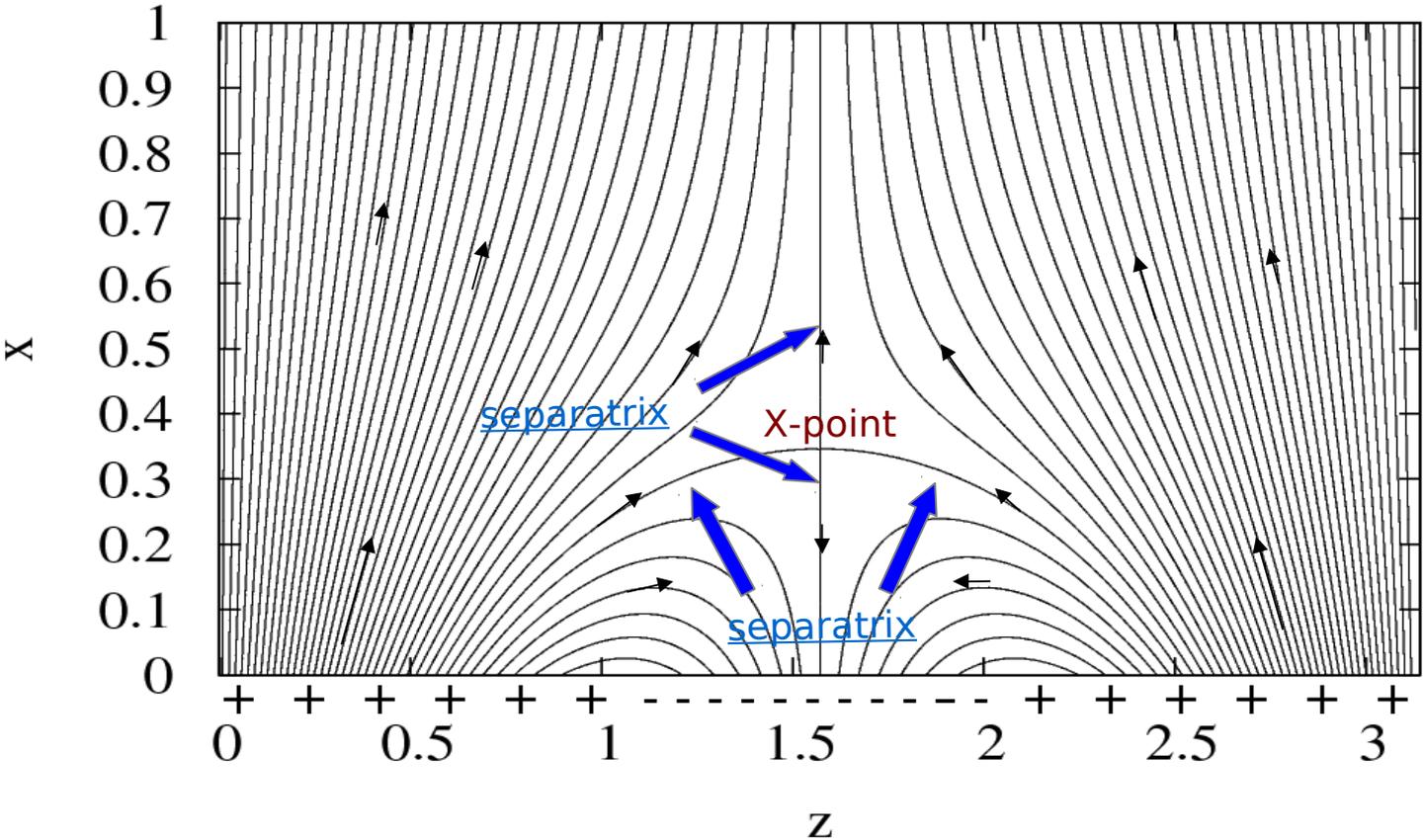
- negligible curvature (cartesian coordinates)

A model for the magnetic field in a coronal hole

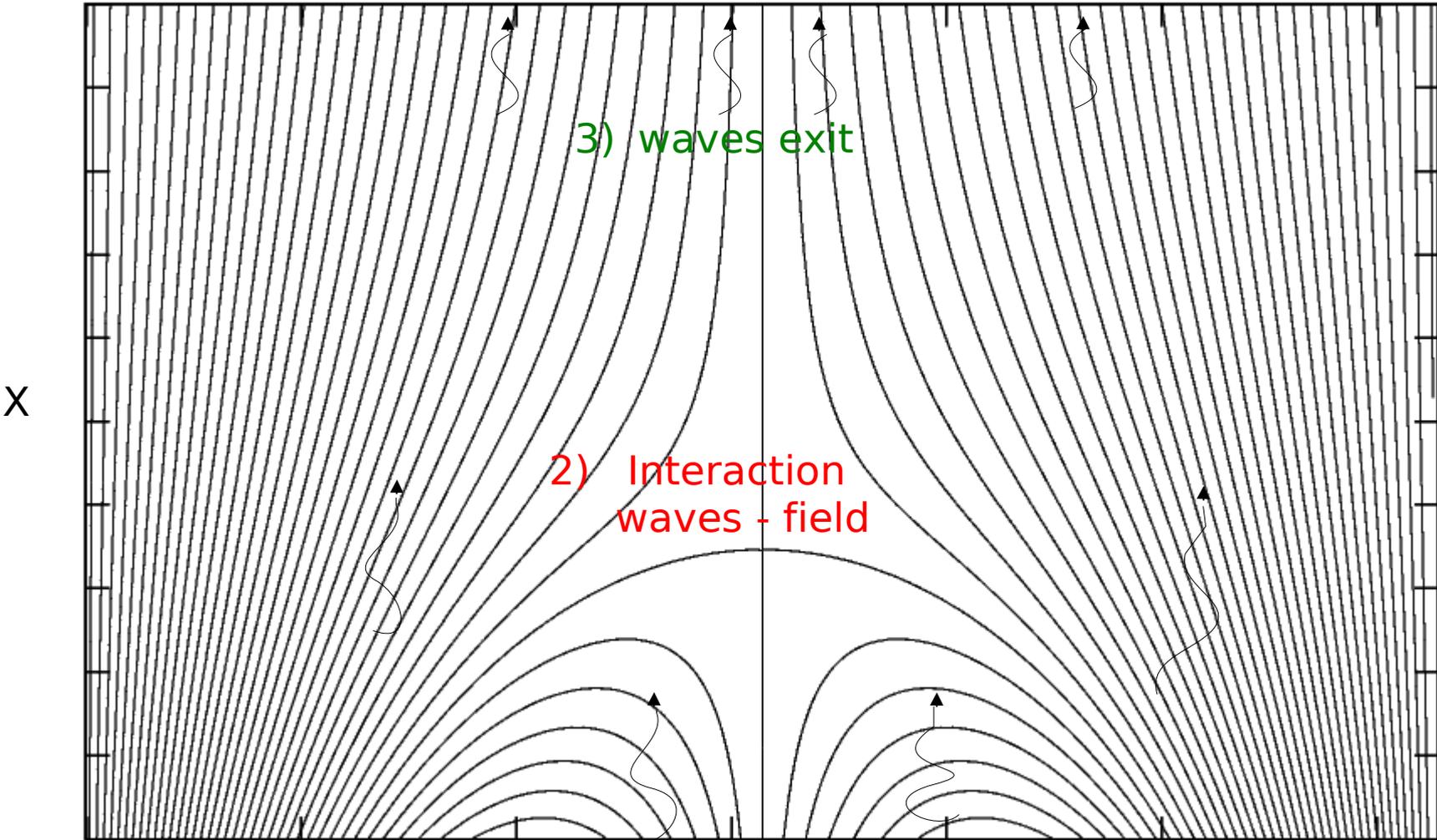
A simple two dimensional solution of the problem is represented by the field:

$$B_x = 2 \cos(2z) e^{-2x} + 1$$

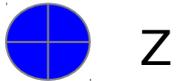
$$B_z = 2 \sin(2z) e^{-2x}$$



What do we do?



1) *Forcing at the boundary*



Z



Alfvénic



Magnetosonic

The MHD equations

$$\frac{\partial \rho}{\partial \tau} + \nabla \cdot (\rho \mathbf{v}) = 0,$$

$$\frac{\partial \mathbf{v}}{\partial \tau} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\frac{1}{\rho} \nabla p + \frac{1}{\rho} (\nabla \times \mathbf{b}) \times \mathbf{b} + \frac{\nu}{\rho} \nabla \cdot \vec{\sigma},$$

$$\frac{\partial \mathbf{b}}{\partial \tau} = \nabla \times (\mathbf{v} \times \mathbf{b}) + \eta \nabla^2 \mathbf{b},$$

$$\frac{\partial p}{\partial \tau} + \nabla \cdot (p \mathbf{v}) + (\gamma - 1) p (\nabla \cdot \mathbf{v}) =$$

$$\kappa \nabla^2 \left(\frac{p}{\rho} \right) + (\gamma - 1) \left[\eta (\nabla \times \mathbf{b})^2 + \frac{\nu}{2} \vec{\sigma} : \vec{\sigma} \right]$$

ρ = ionic density
 \mathbf{v} = velocity
 \mathbf{B} = magnetic field
 P = pressure
 \mathbf{J} = current
 T = temperature
 ν = viscosity
 η = resistivity
 κ = thermic conductivity

All the variables are non dimensional and normalized to these quantities:

$$\rho_0 = 5 \cdot 10^{-16} \text{ g/cm}^3, \quad c_{A0} = 2.5 \cdot 10^7 \text{ cm/s}, \quad B_0 = c_{A0} \sqrt{4\pi \rho_0} = 5.6 \text{ G}$$

$$P_0 = \rho_0 c_{A0}^2 = 0.3 \frac{\text{g}}{\text{cm s}^2}, \quad L_0 = 10^9 \text{ cm}, \quad T_0 = L_0 / c_{A0} = 40 \text{ s}$$

BOUNDARY AND INITIAL CONDITIONS

- periodical boundary conditions along y and z:

$$f(x, 0, z, t) = f(x, 2\pi, z, t) , \forall x \in [0, 1] , \forall z \in [0, \pi] , \forall t \geq 0$$

$$f(x, y, 0, t) = f(x, y, \pi, t) , \forall x \in [0, 1] , \forall y \in [0, 2\pi] , \forall t \geq 0$$

- “characteristics” method implemented on the boundary along the x direction to treat incoming and outgoing perturbations dynamically.

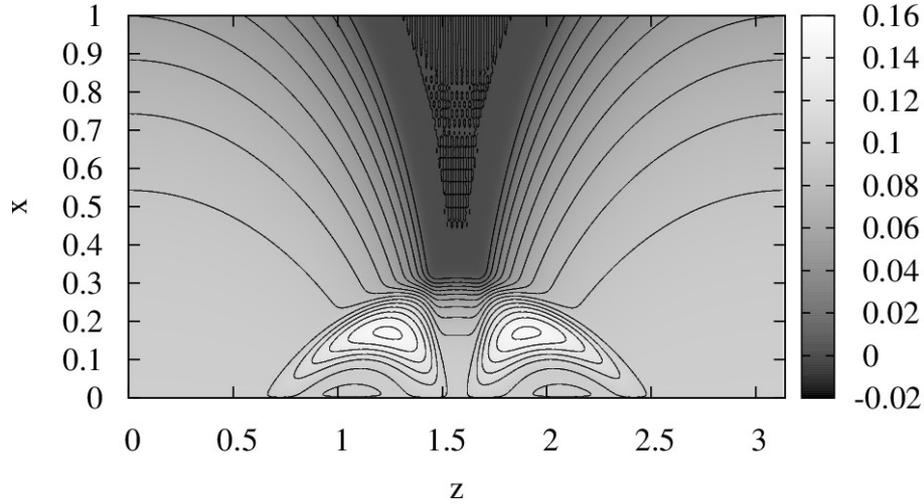
FORCING AT THE BASE OF THE CORONA:

$$\begin{aligned} \mathbf{v}(x = 0, z, \tau) &= v_1 \sin(\omega\tau) \mathbf{e}_y && \text{Alfvénic} && v_1=0.1 \\ &&& && \text{(small amplitude)} \\ &&& && T=160s \\ \mathbf{v}(x = 0, z, \tau) &= v_1 \sin(\omega\tau) \mathbf{e}_z && \text{Magnetosonic} \end{aligned}$$

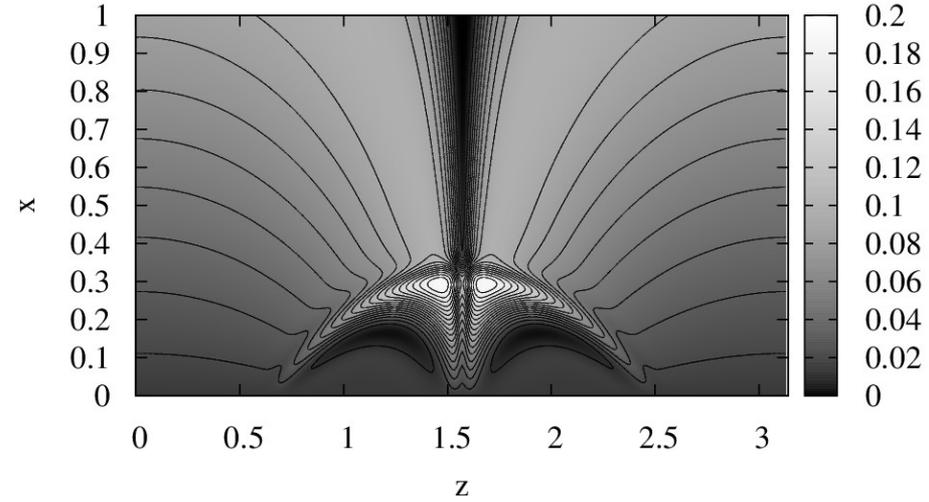
Pressure and density are homogeneous all over the domain at t=0.

Alfvénic mode

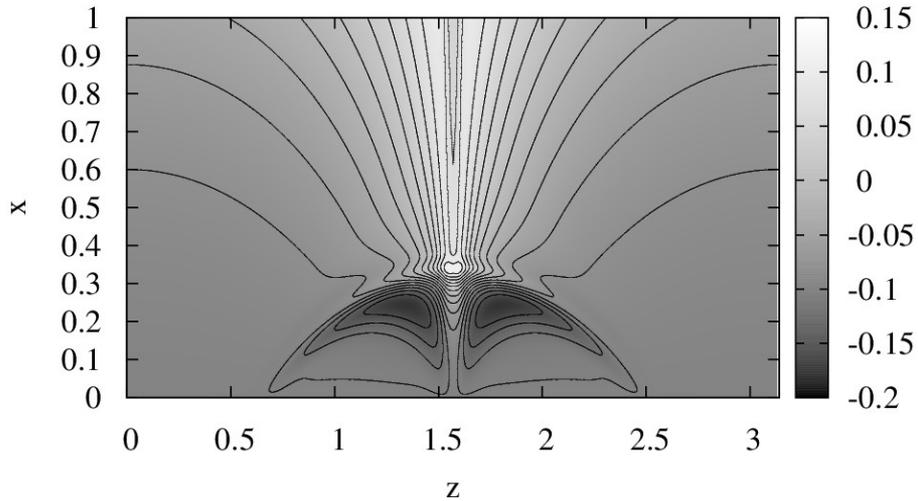
vy (t=1.0)



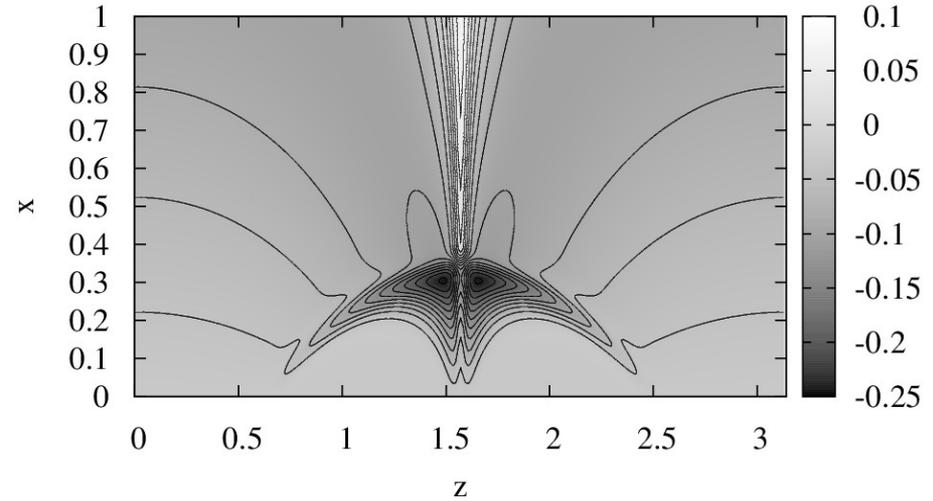
vy (t=2.0)



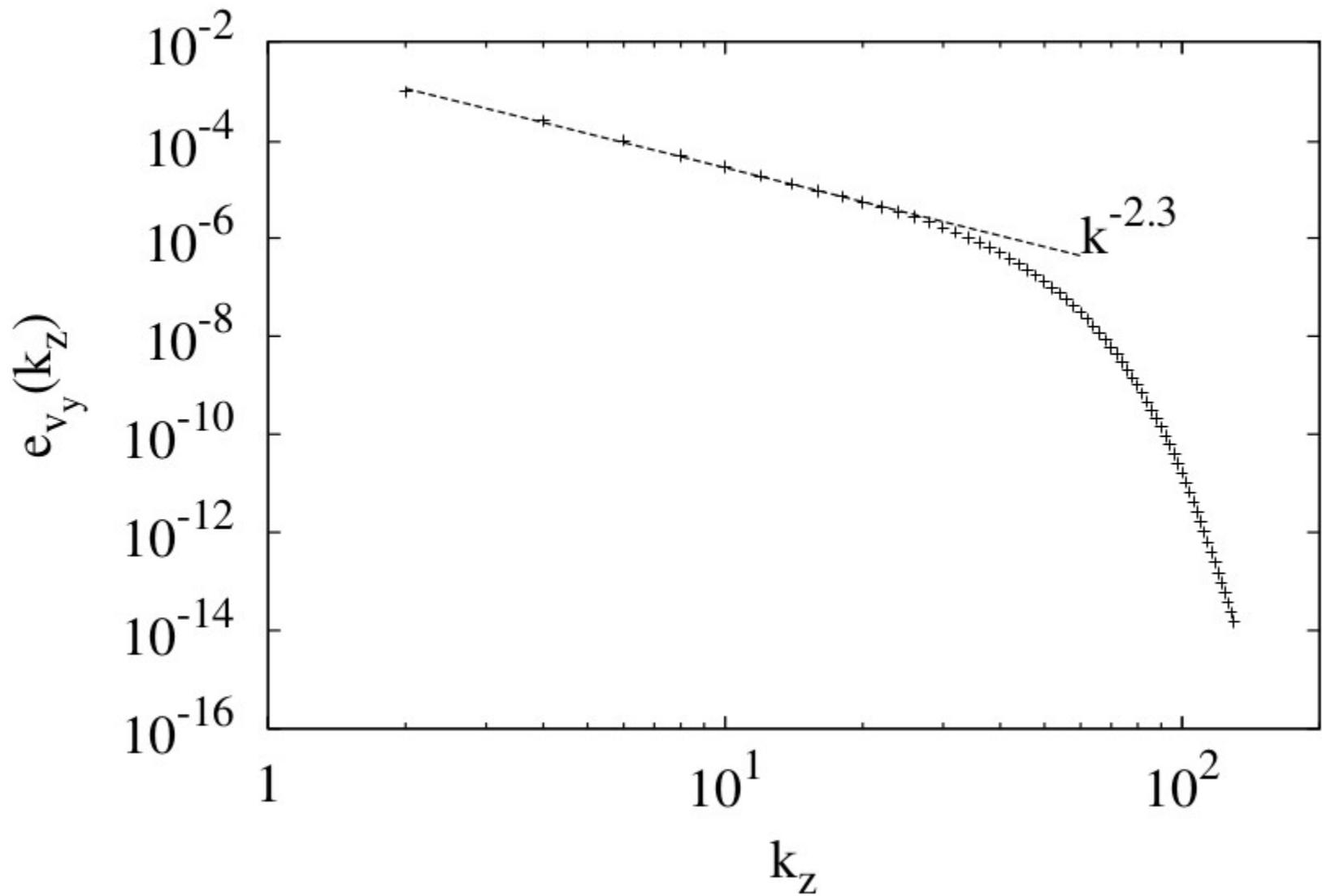
vy (t=3.0)



vy (t=4.0)



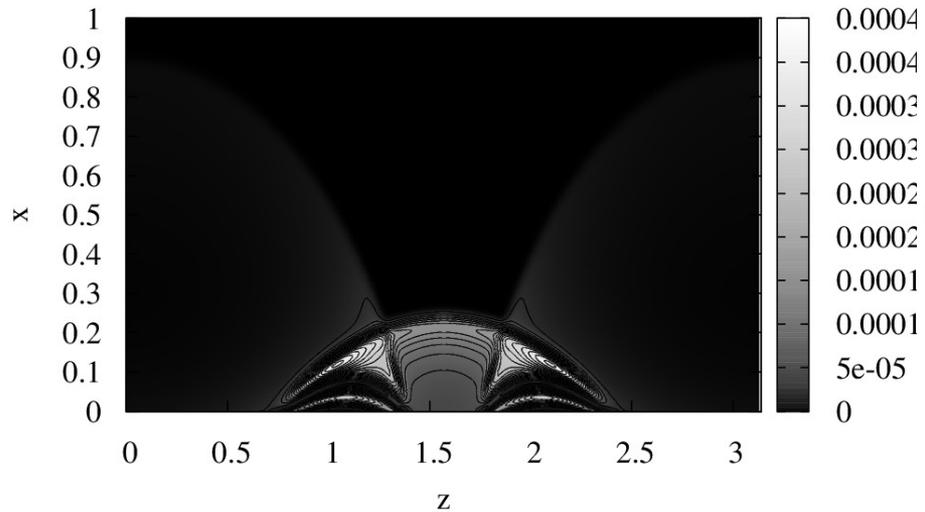
Small scales are concentrated along separatrices



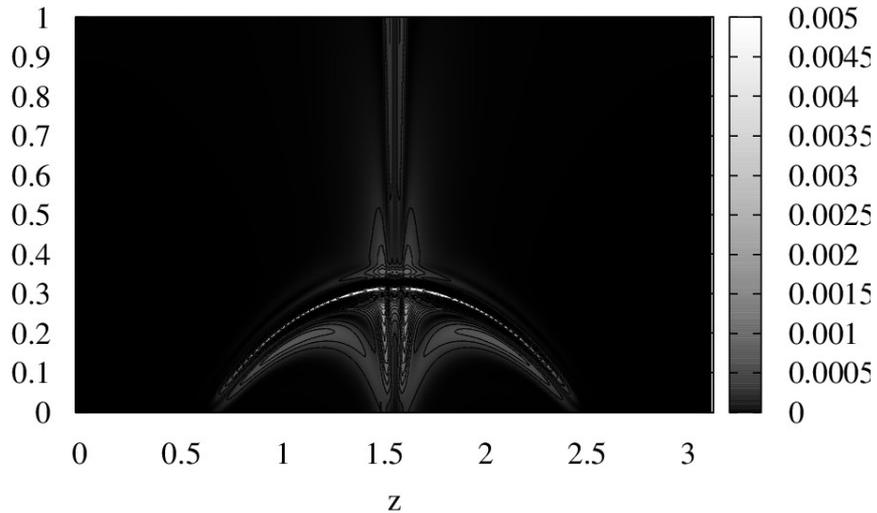
Averaged kinetic energy spectrum of the Alfvénic fluctuation at the top of the domain

Dissipated power

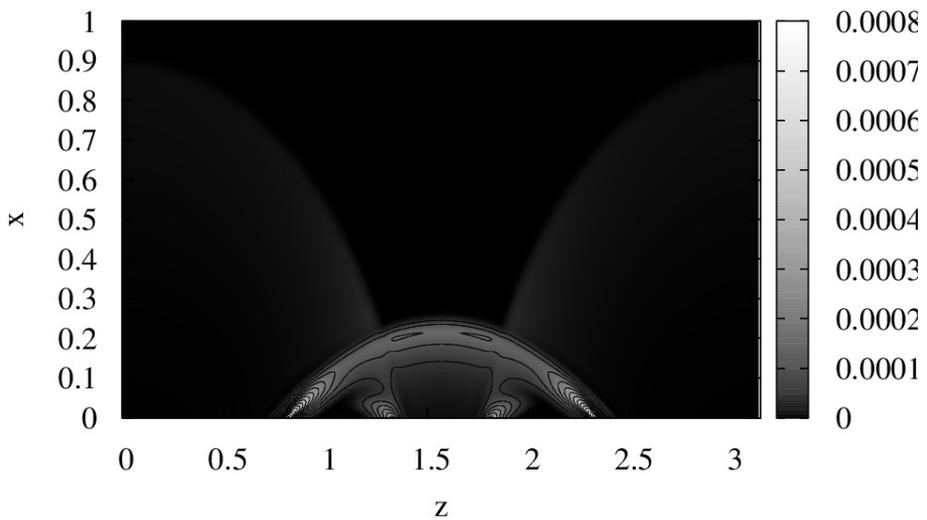
$$(\gamma - 1) \frac{\nu}{2} \sigma_{ij} \sigma_{ij} (t = 0.5)$$



$$(\gamma - 1) \frac{\nu}{2} \sigma_{ij} \sigma_{ij} (t = 3.0)$$

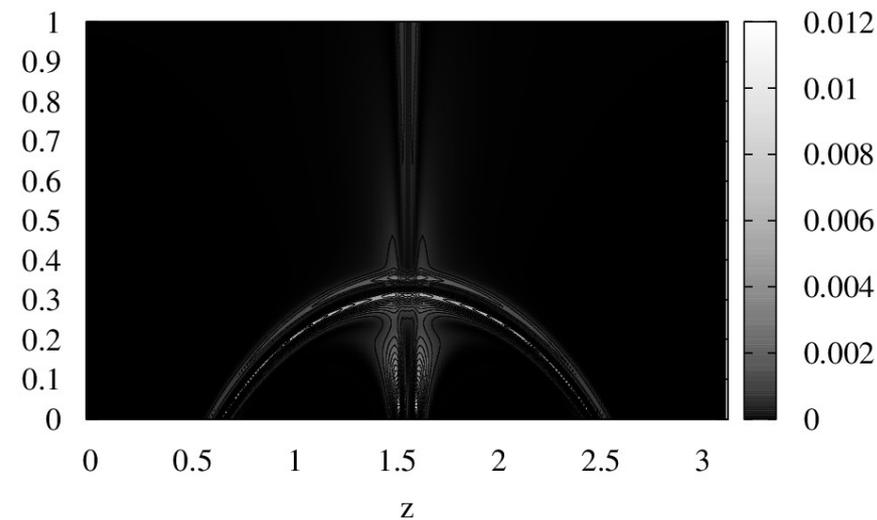


$$(\gamma - 1) \eta J^2 (t = 0.5)$$

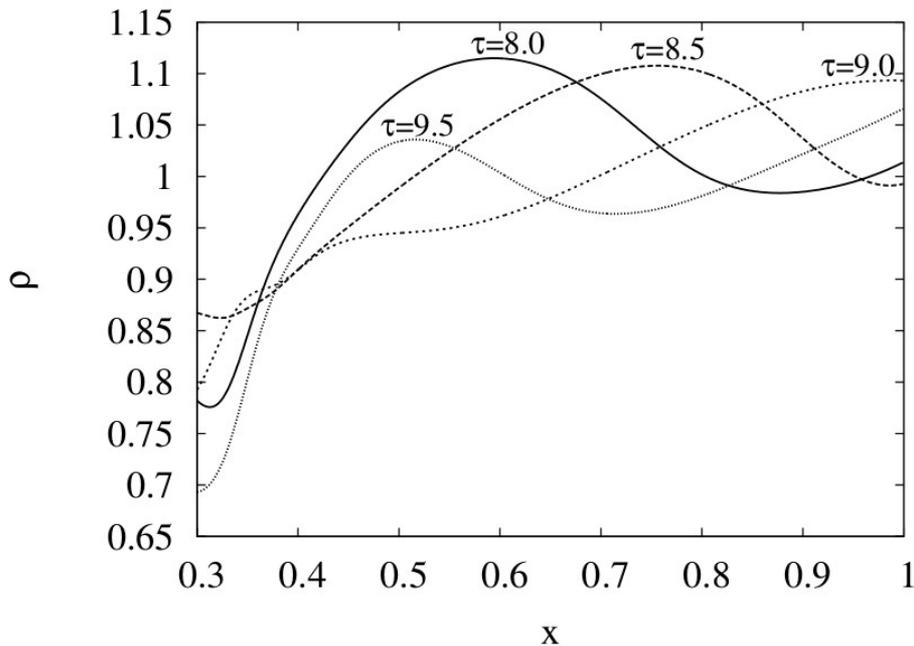
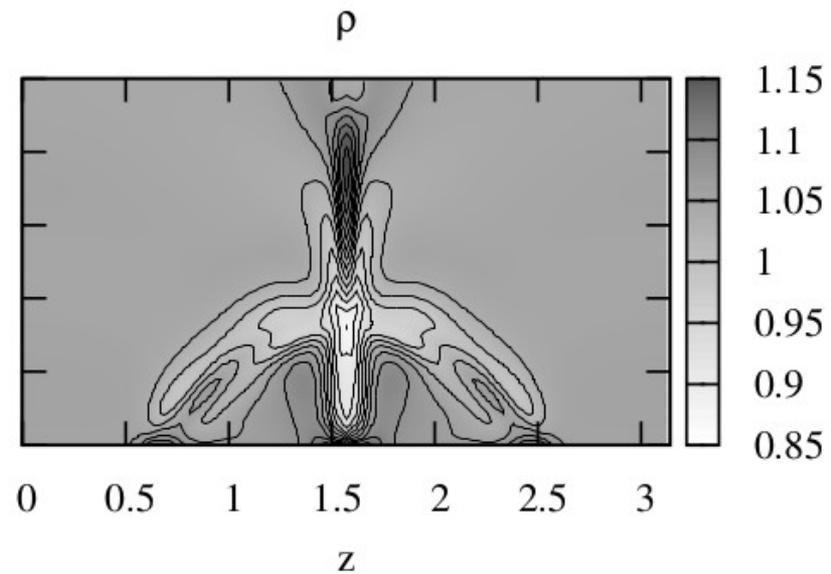
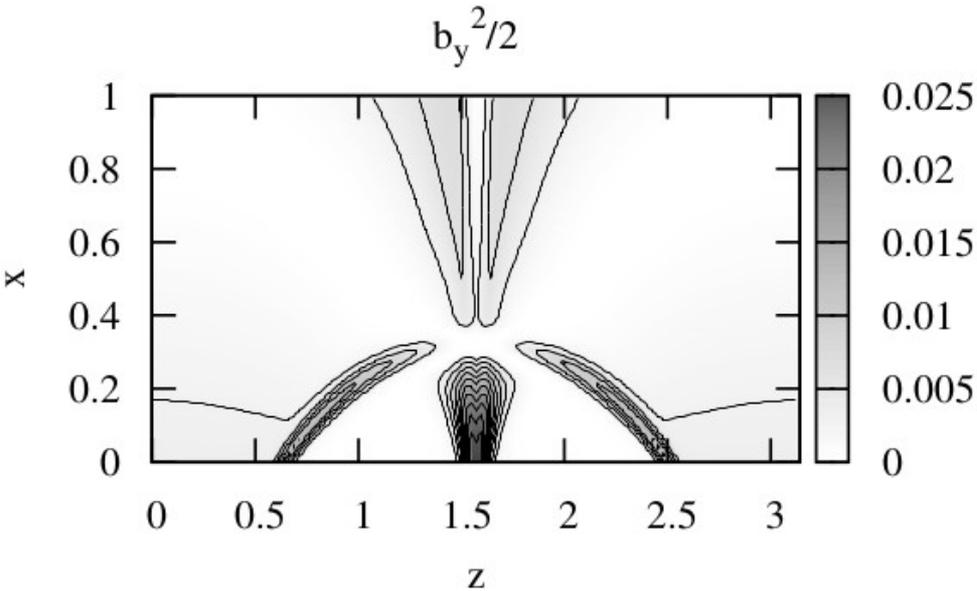


resistive

$$(\gamma - 1) \eta J^2 (t = 3.0)$$



FORMATION AND EJECTION OF PLASMA BUBBLES

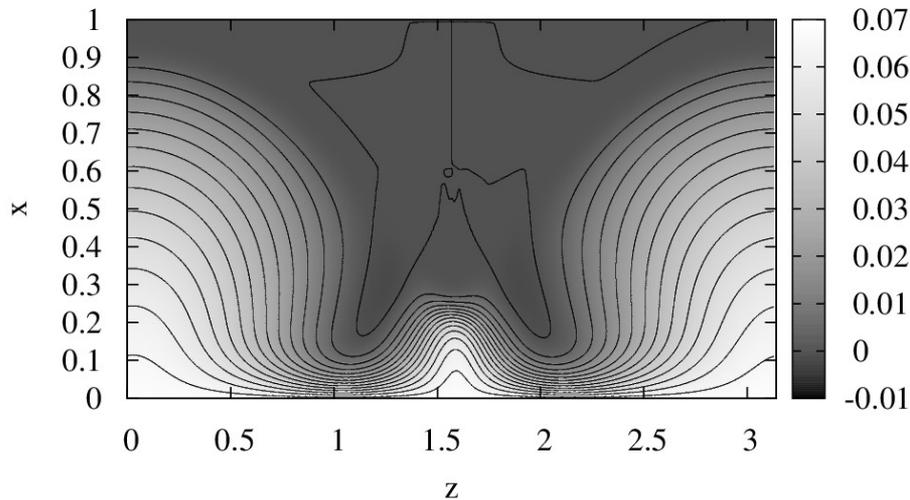


The Alfvén waves push matter toward the middle, generating plasma bubbles that propagate out through the top at a speed comparable to the Alfvén speed.

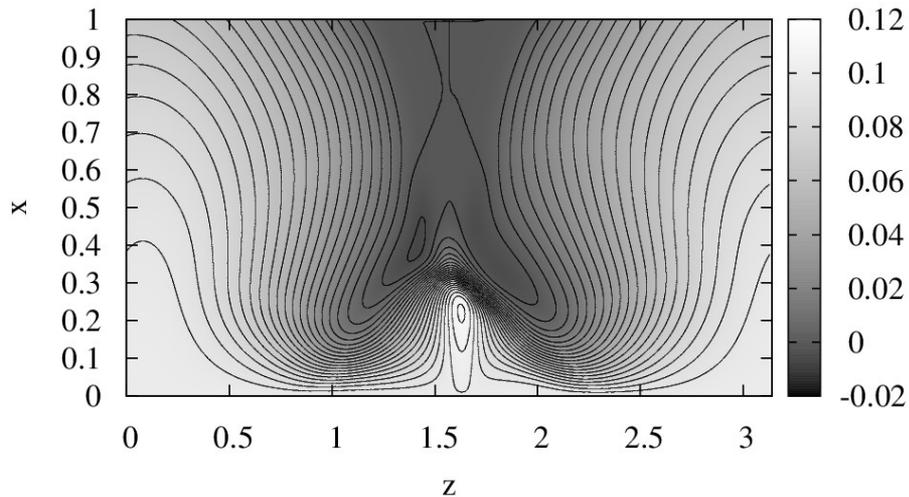
(Pucci et al., 2014)

Magnetosonic mode

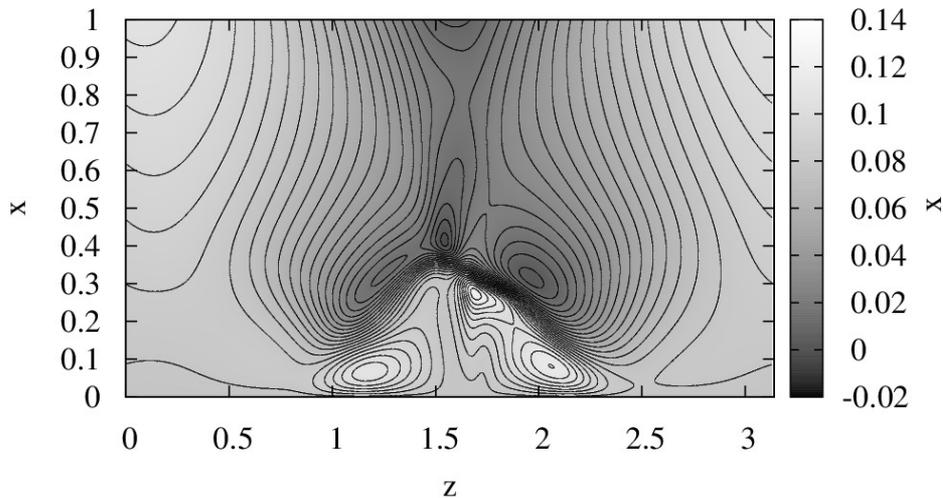
$v_z(t=0.5)$



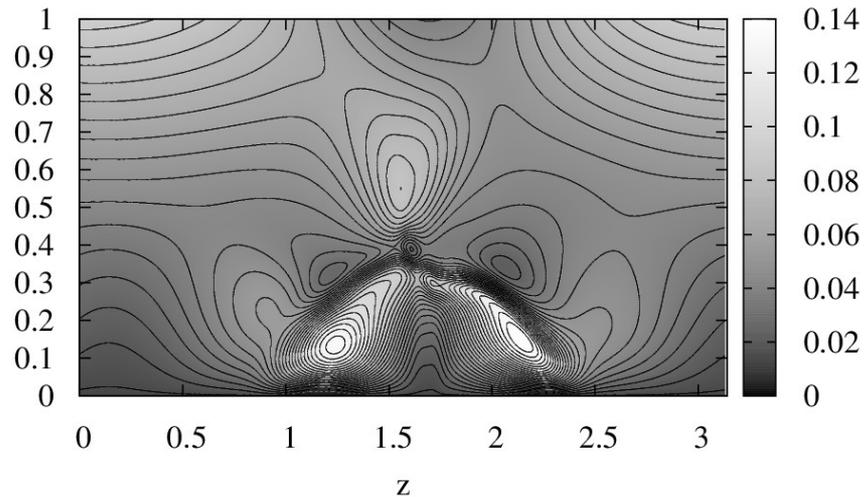
$v_z(t=1.0)$



$v_z(t=1.5)$



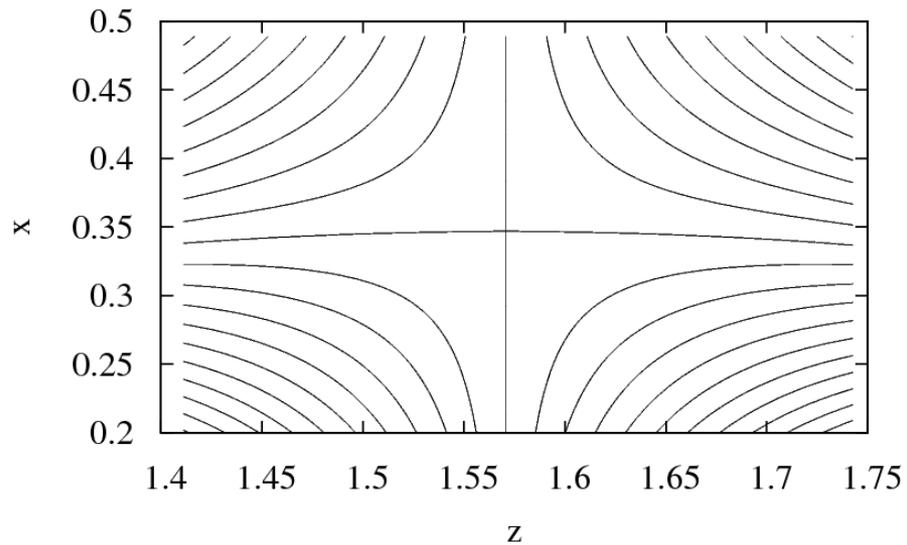
$v_z(t=2.0)$



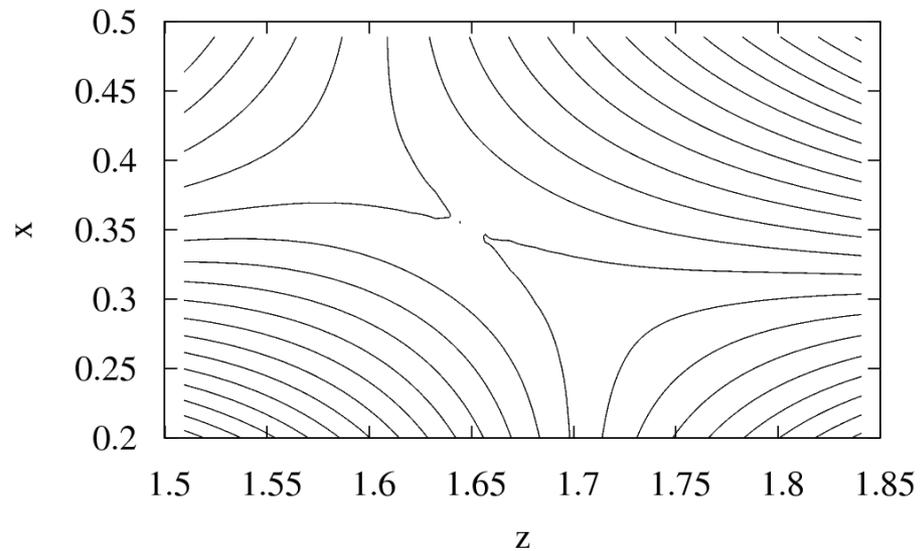
Small scales are concentrated near to the X-point

Magnetic fieldlines (Zoom at the X-Point)

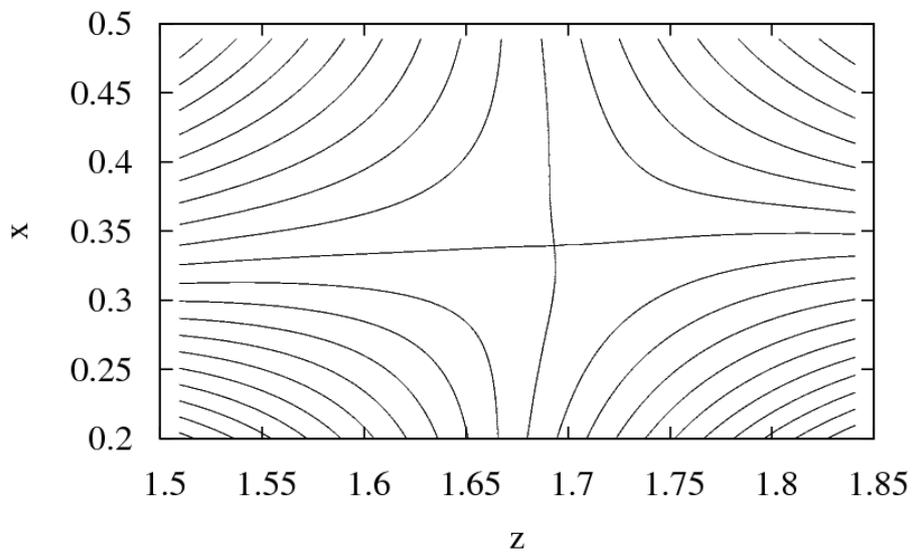
t=0.0



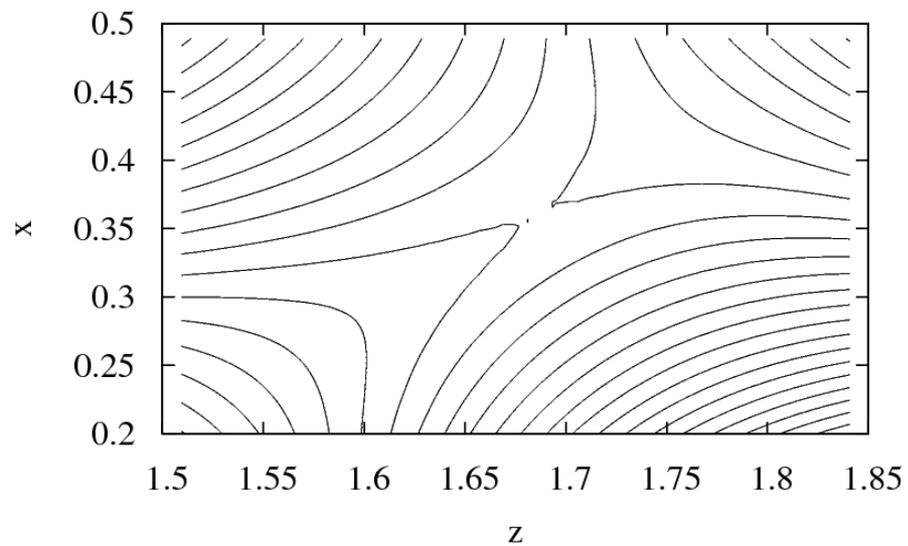
t=2.0



t=2.75

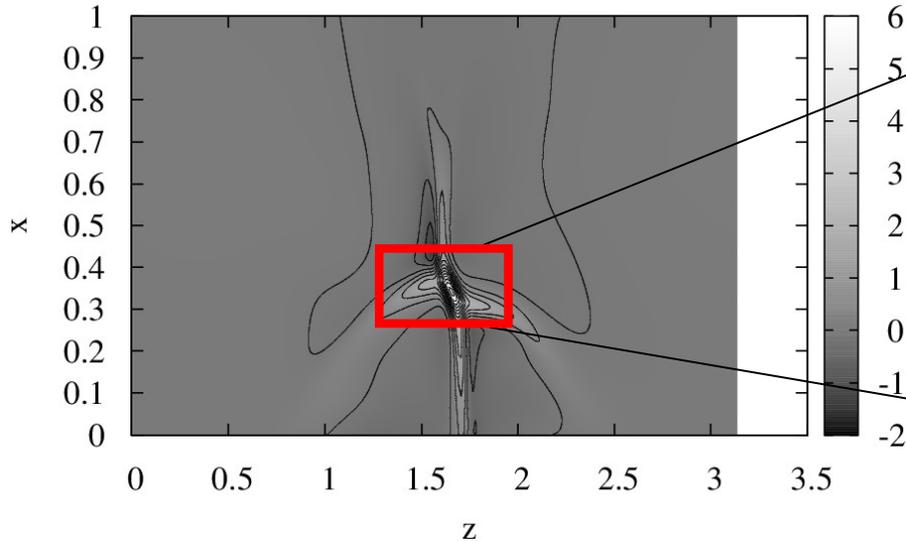


t=3.5

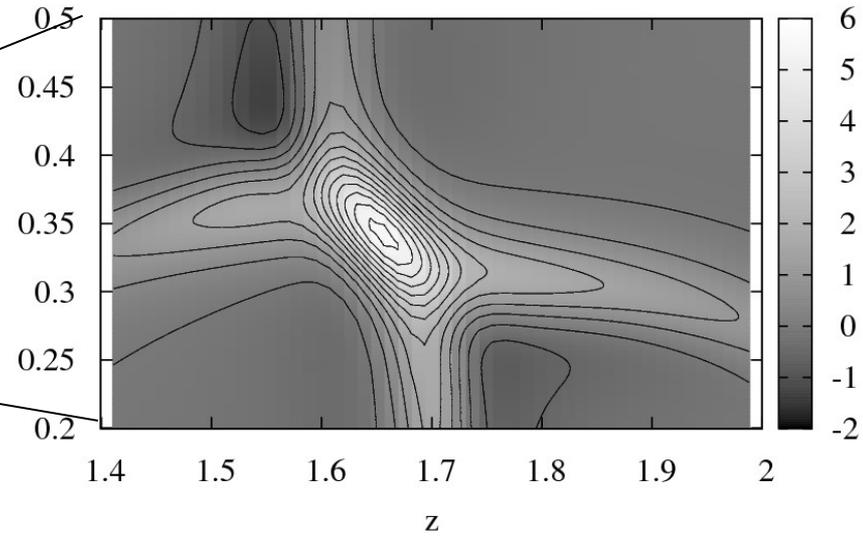


First magnetic reconnection (t=2.0)

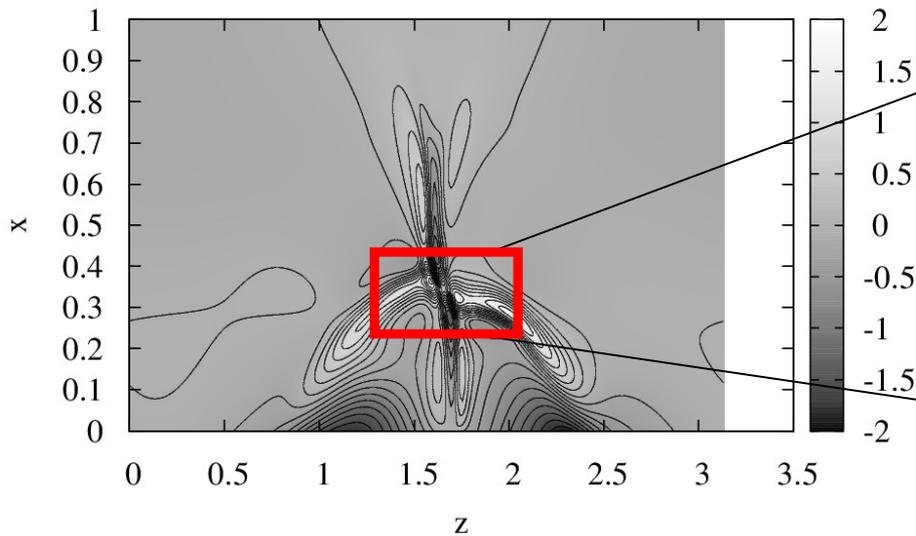
$J_y(t=2)$



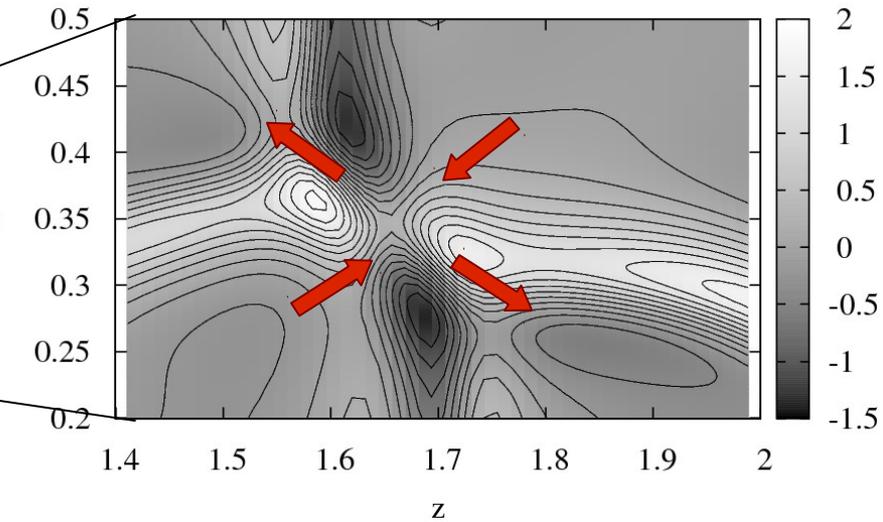
$J_y(t=2)$



$\omega_y(t=2)$

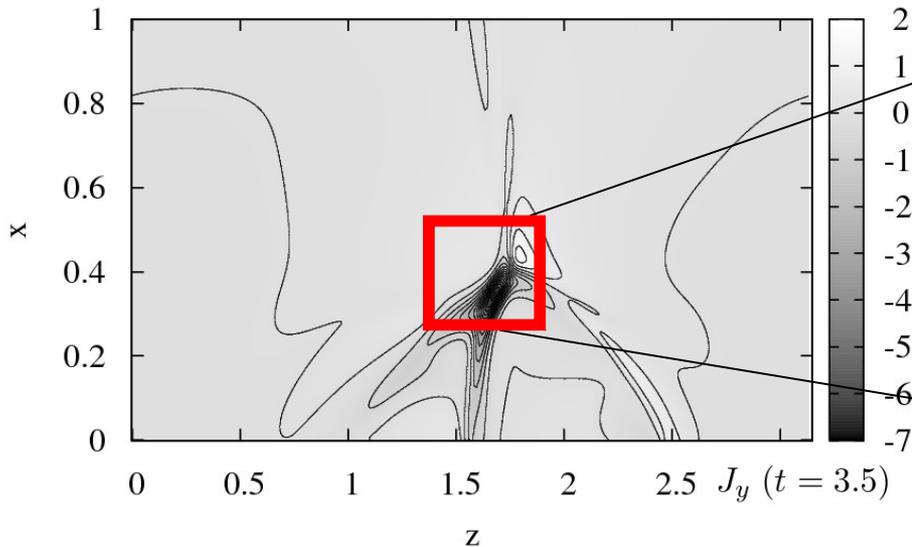


$\omega_y(t=2)$

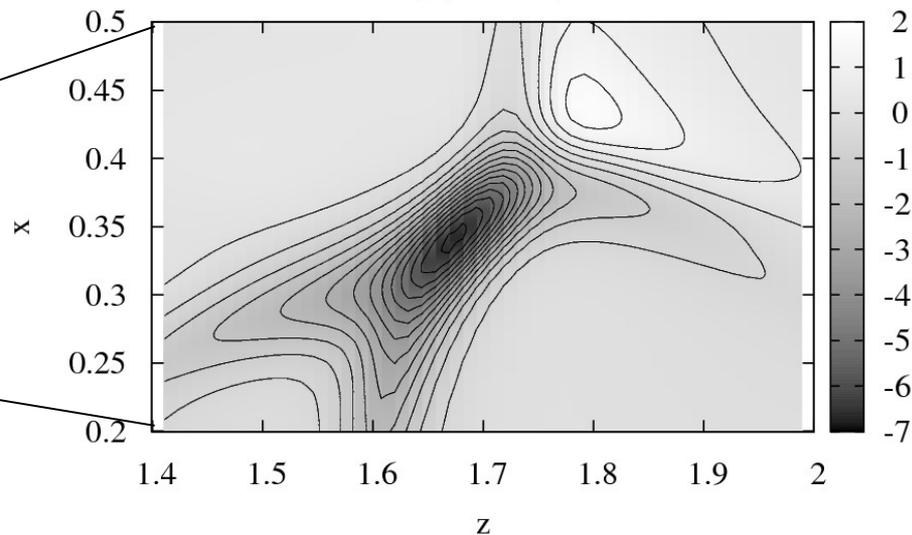


Second magnetic reconnection (t=3.5)

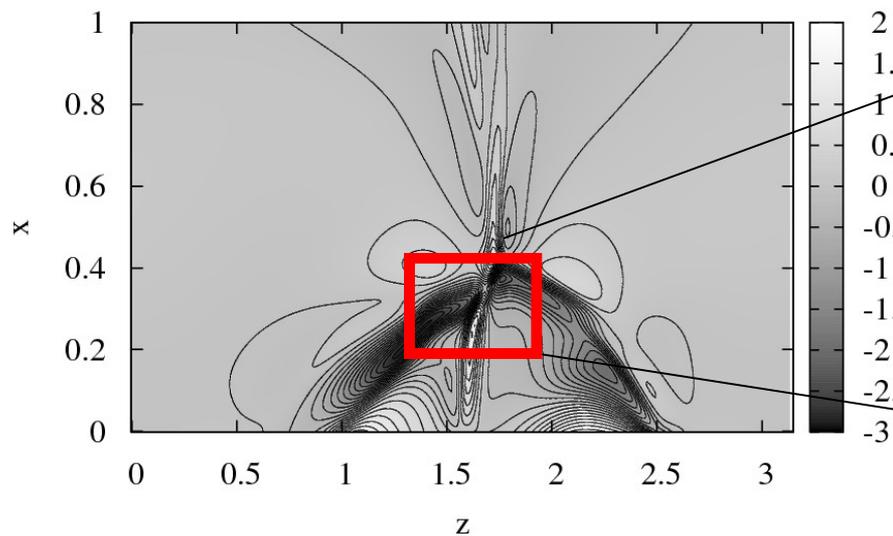
$J_y(t = 3.5)$



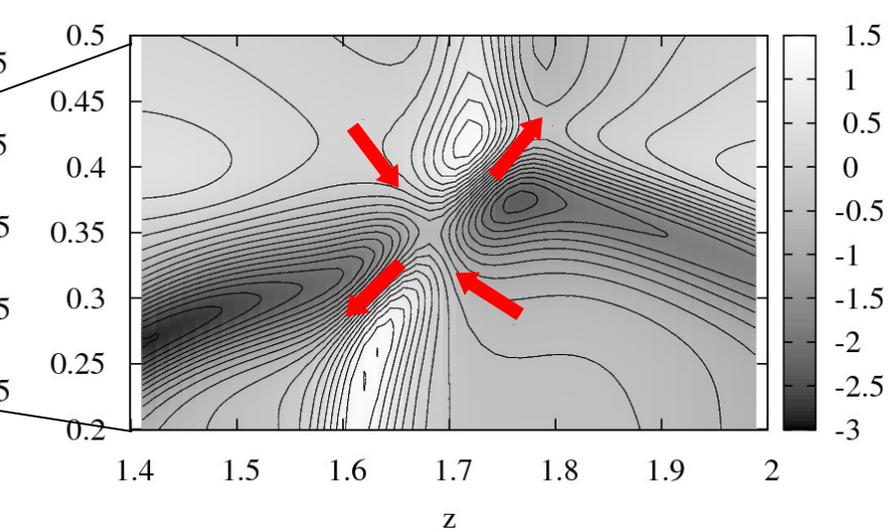
$J_y(t = 3.5)$



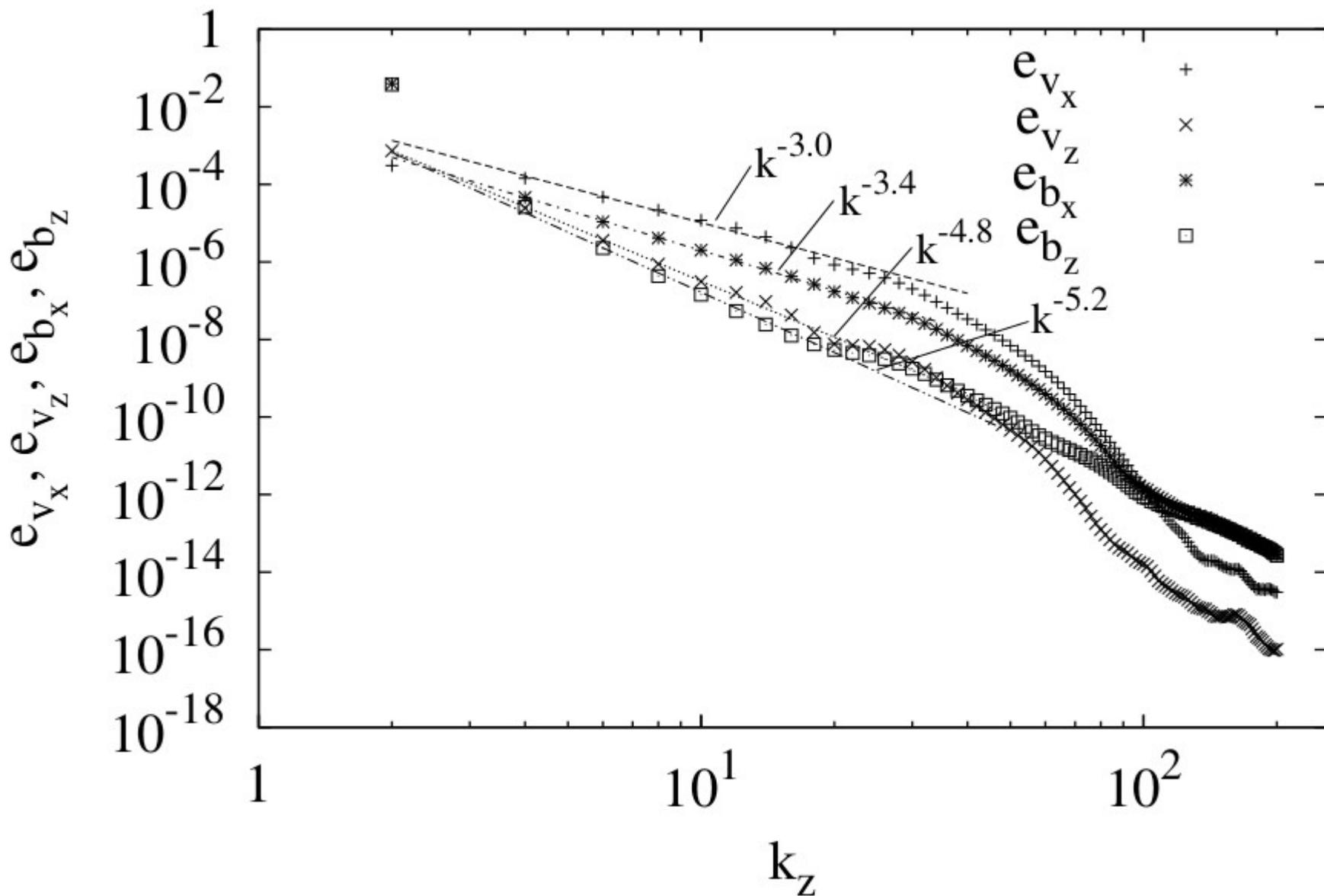
$\omega_y(t = 3.5)$



$\omega_y(t = 3.5)$



Averaged energy spectrum at the top of the domain



Conclusions

- The presence of regions of opposite polarity enhances the small scale formation at low altitudes ($h=10^9$ cm) in a Coronal Hole.
- In the case of the Alfvén perturbation small scales form along separatrix.
- We see the formation of a power law spectrum at the top of the domain for Alfvén perturbation.
- The magnetic pressure due to the Alfvén waves ejects matter towards the outer atmosphere.
- In the case of the Magnetosonic perturbation small scales form in proximity of the X-point, where magnetic reconnection takes place.
- We see a weak formation of small scale at the top of the domain for the Magnetosonic perturbation.

Thank you for your attention