Lunar Dynamical Modeling with Improved IR Lunar Laser Ranging data

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Data Reduction Model : GINS^[6]

Géodésie par Intégrations Numériques Simultanées

- Developed and maintained by OCA-GRGS-CNES
- Time of flight (photon) to Residuals
- Planetary and lunar ephemeris (libration angles)
- Earth orientation (IERS C04 / JPL KEOF)
- Tides and loading
- Tropospheric delay
- Crustal deformation

 (Love & Shida numbers)
- Relativistic effects
- Under study : Hydrology loading



Residuals (m) vs time (year)

Improved IR LLR data

- LASER : Infrared wavelength (1064nm)
- Advantages^[7]:
 - ✓ Better atmospheric transmission
 - ✓ Observations round the clock (high SNR)
 - \checkmark Diversification of observed reflectors
 - Observations during new and full moon \checkmark

Maximum sensitivity for tests of EP : cos(D)





OCA IR Residuals



Preliminary estimates with formal uncertainties from INPOP15b WLS fit

Parameter	INPOP15b	DE430 ^{[1][2]}
Radius Moon km	1.738E+03	1.738E+03
EMRAT	81.3005718	81.3005691±0.0000024
GM_EMB	8.99701159E-10	8.99701139E-10
k2 Moon	2.295E-02 ± 2E-05	2.4059E-02
h2 Moon	1.503E-02 ± 9.9E-05	4.76E-02 ± 6.4E-03
l2 Moon	1.070E-02	1.070E-02
CMR2 Moon	3.928E-01 ± 1.331E-06	3.93142E-01
Gravity field coefficients	GRAIL 660b (BVLS 2 x sig)	GRAIL 660b
C(2,0) Core	-8.501E-08 ± 3.052E-10	-6.78E-08 (computed)
CMR2 Core	6.006E-04 ± 2.771E-06	2.75E-04 (computed)
K CMB	5.560E-09 ± 1.167E-11	6.43E-09
Angular velocities	6.255E-03 ± 2.544E-06	-2.4199E-03
	-4.147E-04 ± 1.232E-06	4.110195E-01
	-8.040E-04 ± 5.090E-06	-4.630947E-01
Cf/C ratio	1.5E-03 ± 7.060E-06 (computed)	7E-04

*bold : fixed parameters

Future work

Current assumptions

- Axial symmetry of liquid core
- Non-differential rotation
- Shape constrained by CMB
- Only viscous drag at CMB
- No topography at CMB

Discussions

- Introduction of inner solid core^[8]
- Electromagnetic coupling^[8]
- Interaction at ICB^[8]

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 [8] Wieczorek, M. et al (2016)